

Contributions to Particle Filters

and Sequential Monte Carlo Methods

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15+ papers · 19 years · 3 core themes · 2007–2026

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Five Research Phases

- I Early Foundations** 2007–08
Sequential simulation for SV & DSGE
- II Particle Learning** 2010–11
Core PL framework — landmark papers
- III Surveys & Extensions** 2012–16
Reviews, new model classes
- IV PL for Stoch. Volatility** 2018–19
Jumps, semi-parametric SV
- V Recent Directions** 2026
Count data, generative connections

Three Interlocking Themes

(1) Particle Learning (PL)

A new SMC paradigm carrying sufficient statistics in particles for exact sequential parameter updates.

(2) Stochastic Volatility (SV)

Online Bayesian inference for time-varying financial risk: Markov switching, jumps, factor models.

(3) Survey & Pedagogy

Multiple review articles and book chapters making SMC accessible to econometricians and statisticians.

SMC

SMC / Particle Filter methodology

SV

Stochastic Volatility application

SURVEY

Survey / Introduction / Pedagogical

PL

Particle Learning framework

APP

Other applied domain



Landmark / invited paper

2007 Markov Switching SV SMC; SV

Simulation-based Sequential Analysis of Markov Switching Stochastic Volatility Models
with Carvalho *Computational Statistics and Data Analysis*, 51, 4526–4542

- ▶ Sequential particle filter for regime-switching volatility — first major SMC paper.
- ▶ Establishes the resample-propagate workflow that Particle Learning later formalises.

2008 DSGE Models SMC; APP

Sequential Monte Carlo Estimation of DSGE Models
with Chen & Petralia *Technical Report*, U. of Chicago Booth

- ▶ Demonstrates SMC in macroeconomic structural models.
- ▶ Shows online posterior tracking works beyond finance.

★ 2010 Particle Learning and Smoothing

Particle Learning and Smoothing

with Carvalho, Johannes & Polson

Statistical Science, 25, 88–106

- ▶ **Foundational paper** of the Particle Learning (PL) framework.
- ▶ Particles carry sufficient statistics; propagation = sequential parameter *and* state learning.
- ▶ Introduces smoothing within PL — cleaner than MCMC, more principled than IS.

★ 2010 PL for General Mixtures

Particle Learning for General Mixtures

with Carvalho, Polson & Taddy

Bayesian Analysis, 5, 709–740

- ▶ Extends PL to mixture models and Dirichlet Process mixtures.
- ▶ Sequential nonparametric Bayesian inference — mixture allocations updated online.

★ 2011 PL — Invited Paper with Discussion PL; SMC

Particle Learning for Sequential Bayesian Computation (with discussion)

with Carvalho, Johannes & Polson

Bayesian Statistics 9, 317–360

- ▶ Comprehensive exposition of PL at the Valencia/ISBA World Meeting.
- ▶ Theory, resample-propagate algorithms, and comparisons to other SMC methods.
- ▶ **Considered a seminal reference** for the PL literature.

2011 Factor Models PL; APP

Dynamic Stock Selection Strategies: A Structured Factor Model Approach (with discussion)

with Carvalho & Aguilar *Bayesian Statistics 9*

- ▶ PL for dynamic factor models in portfolio management.

2011 Epidemic Tracking SMC; APP

Tracking Epidemics with Google Flu Trends and a State-Space SEIR Model

with Dukic & Polson *JASA*, 107, 1410–1426

- ▶ Particle filter for real-time epidemic surveillance.
- ▶ SMC beyond finance — public health impact.

★ 2011 Finance Survey SMC; SV; SURVEY

Particle Filters and Bayesian Inference in Financial Econometrics

with Tsay

Journal of Forecasting, 30, 168–209

- ▶ Comprehensive survey: SIR filters, auxiliary PF, parameter learning in SV & factor models.
- ▶ Includes R implementations — widely used as a course text.
- ▶ [R example scripts available online](#)

2010 Credit Crisis SMC; SV; APP

Extracting SP500 and NASDAQ Volatility: The Credit Crisis of 2007–2008

with Polson

Handbook of Applied Bayesian Analysis (O'Hagan & West, Eds.), 319–342

- ▶ High-profile chapter: SMC tracking of volatility regimes during the 2008 financial crisis.
- ▶ Demonstrates the practical power of online Bayesian filtering.

2012 Resampling Perspective SMC SURVEY

Bayesian Statistics with a Smile: A Resampling-Sampling Perspective
with Polson & Carvalho *BJPS*, 26, 358–371

- Unifies bootstrap, resampling and particle methods under a common Bayesian lens.
- Accessible intuition for why SMC works.

2013 Introduction to PF SMC SURVEY

Online Bayesian Learning in Dynamic Models: An Illustrative Introduction to Particle Methods
with Carvalho *Bayesian Theory and Applications* (Oxford UP), 203–228

- Pedagogical chapter: filtering, smoothing, parameter learning with worked examples.

2013 Comparative Study SMC SV SURVEY

Evaluation and Analysis of Sequential Parameter Learning Methods in Markov Switching SV Models
with Rios *State-Space Models in Economics and Finance* (Springer), 23–61

- Systematic comparison of PL vs. competing particle methods in regime-switching volatility.

2013 Sequential AR Models SMC APP

Sequential Parameter Learning and Filtering in Structured AR Models
with Prado *Statistics and Computing*, 23, 43–57

- PL extended to autoregressive models with structured priors.

2016 PL for Fat Tails PL SMC

Particle Learning for Fat-Tailed Distributions
with Polson *Econometric Reviews*, 35, 1666–1691

- PL augmented for Student- t / stable error distributions.
- Direct applications to financial return modelling.

2018 Variance-Gamma Jumps (with discussion) PL;SV;SMC

Sequential Bayesian Learning for Stochastic Volatility with Variance-Gamma Jumps in Returns
with Warty & Polson *Applied Stochastic Models in Business and Industry*, 34, 460–483

- ▶ Sequential / particle-based inference for SV models with variance-gamma jump component.
- ▶ Discussion format (with two discussions + rejoinder) signals methodological significance.
- ▶ PL robustness demonstrated in the presence of non-Gaussian, jump-driven returns.

2019 Semi-Parametric SV PL;SV;SMC

Particle Learning for Bayesian Semi-Parametric Stochastic Volatility Model
with Virbickaite, Ausín & Galeano *Econometric Reviews*, 38, 1007–1023

- ▶ Fuses PL with Dirichlet Process priors for a semi-parametric SV model.
- ▶ Online inference: nonparametric flexibility + PL efficiency — a genuine methodological hybrid.

2026 Count Time Series SMC; APP

MCMC and Particle Filtering for Dynamic INAR Processes

with Soyer & Zhang

Applied Stochastic Models in Business and Industry (accepted)

- ▶ Particle filtering for integer-valued autoregressive (INAR) count-data models.
- ▶ Applications: insurance claim counts, epidemiology, operations.
- ▶ Compares MCMC and PF for dynamic parameter estimation in a non-Gaussian discrete setting.

2026 Foundations SMC; SURVEY

Uncertainty Quantification: From Weighted Bootstrap to Generators

with Polson & Sokolov

Technical Report

- ▶ Revisits conceptual roots of particle / bootstrap methods.
- ▶ Connects the weighted bootstrap — a core SMC building block — to modern **generative models** (diffusion, VAEs, normalising flows).
- ▶ Positions SMC as a bridge between classical resampling and deep generative AI.

Chronological Timeline



Summary: Key Papers at a Glance

Year	Paper (short title)	Venue	Tags	Lmk
2007	Markov Switching SV (with Carvalho)	CSDA 51	SMC; SV	
2010	Particle Learning & Smoothing	<i>Stat. Sci.</i> 25	PL; SMC	★
2010	PL for General Mixtures	<i>BA</i> 5	PL; SMC	★
2011	PL — Valencia invited (disc.)	<i>BS9</i>	PL; SMC	★
2011	PF in Financial Econometrics	<i>JoF</i> 30	SMC; SV; SURVEY	★
2011	SEIR Epidemic Tracking	<i>JASA</i> 107	SMC; APP	
2012	Bayesian Statistics with a Smile	<i>BJPS</i> 26	SMC; SURVEY	
2013	Introduction to Particle Methods	Oxford UP	SMC; SURVEY	
2013	Sequential AR Models	<i>Stat. Comp.</i> 23	SMC	
2016	PL for Fat-Tailed Distributions	<i>Econ. Rev.</i> 35	PL; SMC	★
2018	SV with VG Jumps (disc.)	<i>ASMBI</i> 34	PL; SV	
2019	Semi-Parametric SV	<i>Econ. Rev.</i> 38	PL; SV	
2026	PF for Dynamic INAR	<i>ASMBI</i> (acc.)	SMC; APP	
2026	Bootstrap to Generators	Tech. Report	SMC; SURVEY	

PL Particle Learning SMC SMC/PF SV Stoch.Volatility APP Application SURVEY Survey ★ Landmark

(1) Particle Learning



- ▶ Sufficient statistics in particles
- ▶ Resample-propagate algorithm
- ▶ Exact sequential parameter learning
- ▶ Smoother than MCMC on long series

Key papers: Stat. Sci. 2010, BA 2010, BS9 2011, ER 2016

(2) Stochastic Volatility



- ▶ Markov switching regimes (2007)
- ▶ Factor SV & portfolio (2011)
- ▶ Jump-driven returns (2018)
- ▶ Semi-parametric DP prior (2019)

Key papers: CSDA 2007, JoF 2011, ASMBI 2018, ER 2019

(3) Survey & Pedagogy



- ▶ JoF 2011: finance tutorial with R
- ▶ Oxford UP 2013: chapter intro
- ▶ BJPS 2012: conceptual essay
- ▶ 2026: SMC to generative models

Consistent effort to broaden the SMC community

Thank you

Full paper list and PDFs:

<https://hedibert.org/scientific-papers/>

15 papers on PF / SMC · 2007–2026 · Particle Learning · Stochastic Volatility · Surveys